

Constraining electroweak breaking from exotic scalars using LHC diboson searches

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H.E.L. & V. Rentala, 1502.01275; M.J. Harris & H.E.L., in progress
K. Hartling, K. Kumar, & H.E.L., 1404.2640, 1410.5538, 1412.7387

Outline

Introduction & motivation

The models

Phenomenology & LHC search prospects

Summary & outlook

SM success: triumph of the gauge principle

QED

Precision electroweak

Perturbative QCD / Lattice QCD

CKM picture for flavor physics

SM challenge: mystery of the vacuum

Origin of W , Z masses

Origin of quark & lepton masses, mixing, CP violation

Origin of neutrino masses, mixing

Dark energy / Inflation

Hierarchy

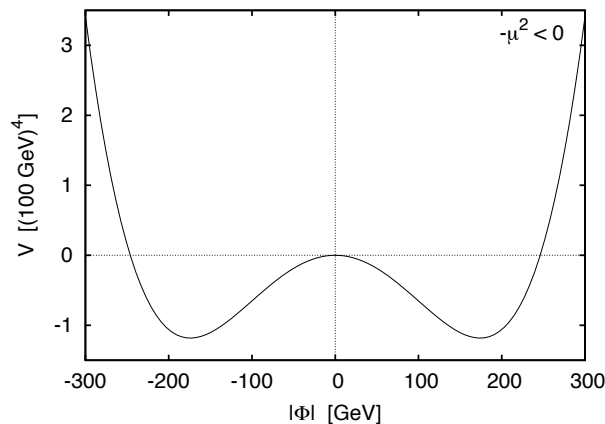
The Standard Model: EWSB from a scalar $SU(2)_L$ doublet

A one-line theory:

$$\mathcal{L}_{Higgs} = |D_\mu \Phi|^2 - [-\mu^2 \Phi^\dagger \Phi + \lambda (\Phi^\dagger \Phi)^2] - [y_f \bar{f}_R \Phi^\dagger F_L + \text{h.c.}]$$

Most general, renormalizable, gauge-invariant theory involving a single spin-zero (scalar) field with isospin 1/2, hypercharge 1.

$-\mu^2$ term: **vacuum condensate!** EW symmetry spontaneously broken; Goldstone bosons gauged away, 1 physical particle h .



$$\Phi = \begin{pmatrix} G^+ \\ (v + h + iG^0)/\sqrt{2} \end{pmatrix}$$

Mass and vacuum expectation value of h are fixed by minimizing the Higgs potential:

$$v^2 = \mu^2 / \lambda$$

$$M_h^2 = 2\lambda v^2 = 2\mu^2$$

The Standard Model: EWSB from a scalar $SU(2)_L$ doublet

SM Higgs couplings to SM particles are fixed by the mass-generation mechanism.

W and Z :

$$g_Z \equiv g / \cos \theta_W = \sqrt{g^2 + g'^2}, \quad v = 246 \text{ GeV}$$

$$\mathcal{L} = |\mathcal{D}_\mu \Phi|^2 \rightarrow (g^2/4)(h+v)^2 W^+ W^- + (g_Z^2/8)(h+v)^2 Z Z$$

$$M_W^2 = g^2 v^2 / 4 \quad h W W : i(g^2 v / 2) g^{\mu\nu}$$

$$M_Z^2 = g_Z^2 v^2 / 4 \quad h Z Z : i(g_Z^2 v / 2) g^{\mu\nu}$$

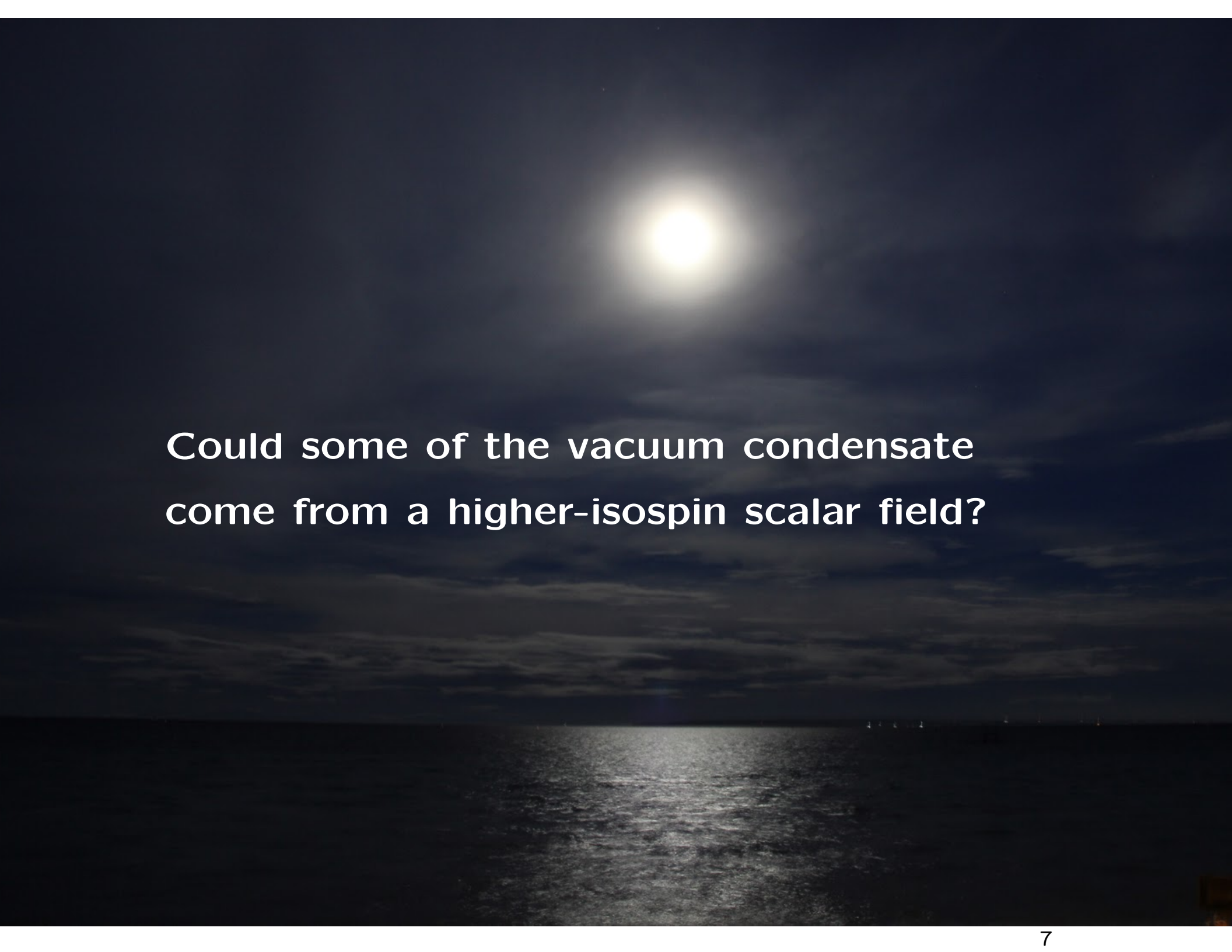
Fermions:

$$\mathcal{L} = -y_f \bar{f}_R \Phi^\dagger F_L + \dots \rightarrow -(y_f / \sqrt{2})(h+v) \bar{f}_R f_L + \text{h.c.}$$

$$m_f = y_f v / \sqrt{2} \quad h \bar{f} f : i m_f / v$$

Gluon pairs and photon pairs:

induced at 1-loop by fermions, W -boson.



**Could some of the vacuum condensate
come from a higher-isospin scalar field?**

Part of vacuum condensate from a higher-isospin scalar field?

Fermion masses can arise only from $SU(2)_L$ doublet(s)

$$\mathcal{L} = -y_f \bar{f}_R \Phi^\dagger F_L + \dots \rightarrow -(y_f/\sqrt{2})(\phi^{0,r} + v_\phi) \bar{f}_R f_L + \text{h.c.}$$
$$m_f = y_f v_\phi / \sqrt{2} \quad \phi^{0,r} \bar{f} f : iy_f / \sqrt{2} = im_f / v_\phi$$

F_L is doublet, f_R is singlet, need Φ doublet for gauge invariance

Top quark Yukawa perturbativity \Rightarrow lower bound on doublet vev:
define $\cos \theta_H \equiv v_\phi / v_{SM}$, then $\tan \theta_H < 10/3$ (or $\cos \theta_H > 0.287$)

Scalar couplings to fermions come from their doublet content

$$\Phi = \begin{pmatrix} \phi^+ \\ (v_\phi + \phi^{0,r} + i\phi^{0,i})/\sqrt{2} \end{pmatrix}$$

With other scalar fields in play, Goldstone bosons are linear combinations of different fields.

Part of vacuum condensate from a higher-isospin scalar field?

W and Z masses arise from anything carrying $SU(2)_L \times U(1)_Y$

$$M_W^2 = \frac{g^2}{4} \sum_k 2 \left[T_k(T_k + 1) - \frac{Y_k^2}{4} \right] v_k^2 = \frac{g^2}{4} v_{SM}^2$$
$$M_Z^2 = \frac{g^2}{4 \cos^2 \theta_W} \sum_k Y_k^2 v_k^2 = \frac{g^2}{4 \cos^2 \theta_W} v_{SM}^2$$

($Q = T^3 + Y/2$, vevs defined as $\langle \phi_k^0 \rangle = v_k/\sqrt{2}$ for complex reps and $\langle \phi_k^0 \rangle = v_k$ for real reps)

Used $Q = 0$ for component carrying the vev to simplify expressions

Top Yukawa perturbativity $\rightarrow (v_\phi/v_{SM})^2 > (0.287)^2 = 0.082$
 \Rightarrow At least 8.2% of $M_{W,Z}^2$ comes from doublet.

Lots of room for higher-isospin scalar contributions!

Can we constrain this exotic possibility?

Problem with higher-isospin scalar multiplets

$\rho \equiv$ ratio of strengths of charged and neutral weak currents

$$\rho = \frac{M_W^2}{M_Z^2 \cos^2 \theta_W} = \frac{\sum_k 2[T_k(T_k + 1) - Y_k^2/4]v_k^2}{\sum_k Y_k^2 v_k^2}$$

($Q = T^3 + Y/2$, vevs defined as $\langle \phi_k^0 \rangle = v_k/\sqrt{2}$ for complex reps and $\langle \phi_k^0 \rangle = v_k$ for real reps)

PDG 2014: $\rho = 1.000\,40 \pm 0.000\,24$

We can still have higher-isospin scalars with non-negligible vevs;
only two approaches using symmetry: (could also tune ρ by hand, but icky)

1) Impose **global $SU(2)_L \times SU(2)_R$ symmetry** on scalar sector
 \implies breaks to custodial $SU(2)$ upon EWSB; $\rho = 1$ at tree level

Georgi & Machacek 1985; Chanowitz & Golden 1985

2) $\rho = 1$ “by accident” for $(T, Y) = (\frac{1}{2}, 1)$ doublet; $(3, 4)$ **septet**

Septet: Hisano & Tsumura, 1301.6455; Kanemura, Kikuchi & Yagyu, 1301.7303

Larger solutions forbidden by perturbative unitarity of weak charges.

Both have theoretical “issues”:

1) Global $SU(2)_L \times SU(2)_R$ is broken by gauging hypercharge.

Gunion, Vega & Wudka 1991

Special relations among param's of *full* gauge-invariant scalar potential can only hold at one energy scale: violated by running due to hypercharge. Garcia-Pepin, Gori, Quiros, Vega, Vega-Morales, Yu 2014

Need the UV completion to be nearby!

2) Can't give the septet a vev through spontaneous breaking without generating a physical massless Goldstone boson.

Have to couple it to the SM doublet through a dimension-7 $X\Phi^*\Phi^5$ term Hisano & Tsumura 2013

Need the UV completion to be nearby!

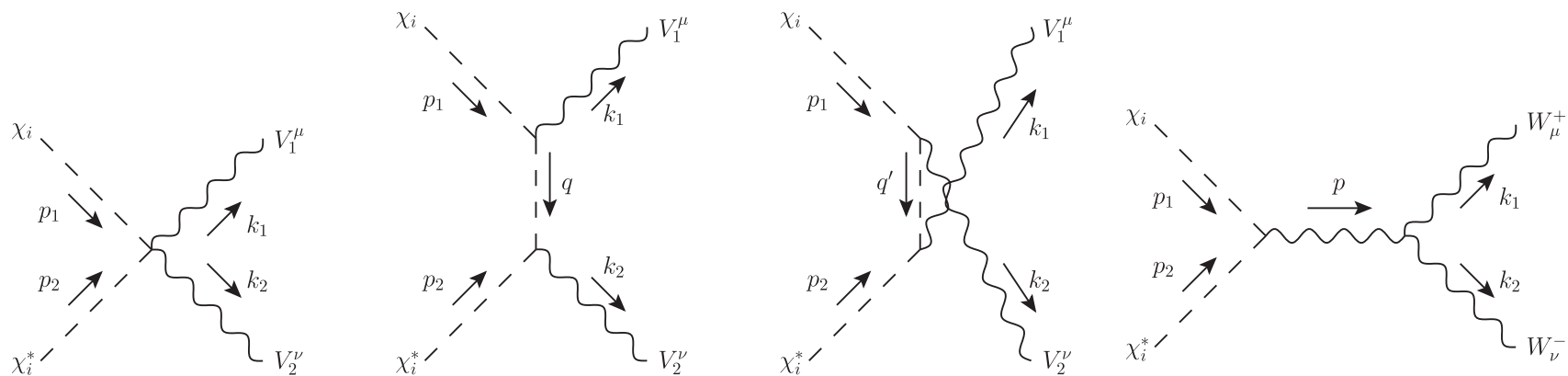
Need UV completion to solve the hierarchy problem anyway!

How large can the isospin be?

Hally, HEL, & Pilkington 1202.5073

Consider $2 \rightarrow 2$ scattering amplitudes for $\phi\phi \rightarrow V_T V_T$:
transverse $SU(2)_L$ gauge bosons

- no growth with E^2 ; amplitude depends on weak charges & number of ϕ 's



How large can the isospin be?

Hally, HEL, & Pilkington 1202.5073

Consider $2 \rightarrow 2$ scattering amplitudes for $V_T V_T \rightarrow \phi\phi$:
transverse $SU(2)_L$ gauge bosons

- no growth with E^2 ; amplitude depends on weak charges & number of ϕ 's

General result for complex scalar multiplet with $n = 2T + 1$:

$$a_0^{\max} = \frac{g^2}{16\pi} \frac{(n^2 - 1)\sqrt{n}}{2\sqrt{3}}$$

- Real scalar multiplet: divide by $\sqrt{2}$ to account for smaller number of ϕ 's
- More than one multiplet: add a_0 's in quadrature

Unitarity: require largest eigenvalue a_0^{\max} satisfies $|\operatorname{Re} a_0| < 1/2$:

- Complex multiplet $\Rightarrow T \leq 7/2$ (8-plet)
- Real multiplet $\Rightarrow T \leq 4$ (9-plet)
- Constraints tighter if more than one large multiplet is present

(generally required in $SU(2)_L \times SU(2)_R$ -symmetric models)

Essentially a requirement that the weak charges not be too large.

The models

1) Models with global $SU(2)_L \times SU(2)_R$ symmetry:

a) Georgi-Machacek model

b) Generalizations to higher isospin

2) Model with a scalar septet

All these models share a key common feature:

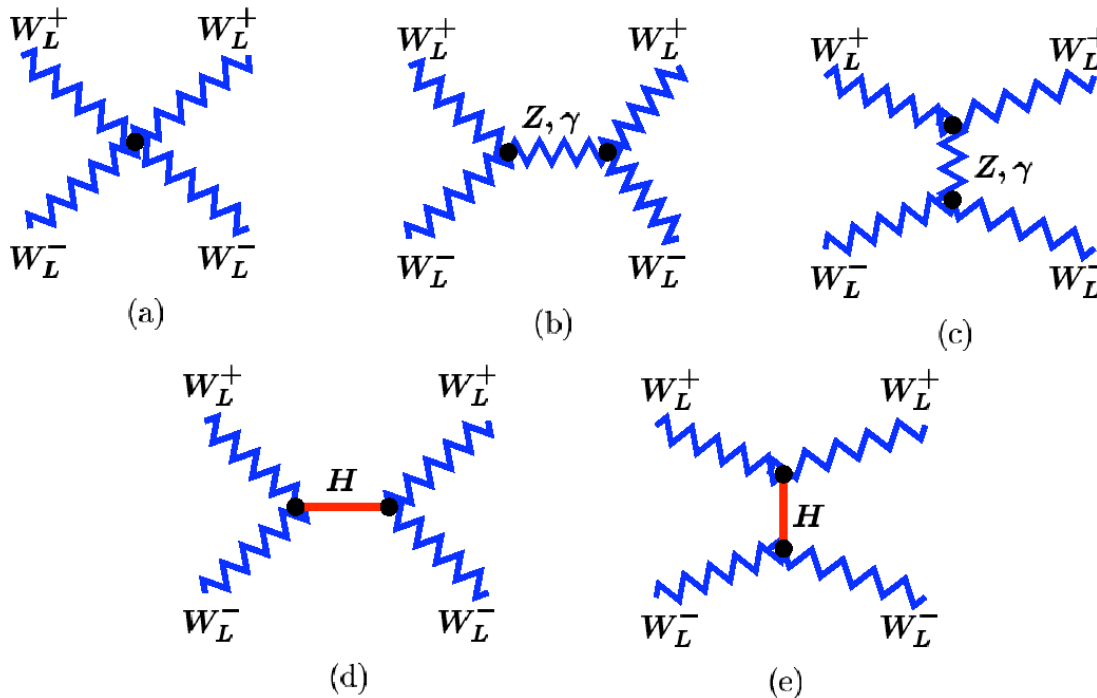
$$H^{\pm\pm} \leftrightarrow W^{\pm}W^{\pm} \text{ and } H^{\pm} \leftrightarrow W^{\pm}Z$$

with couplings controlled by vev of higher-isospin scalar(s)

Generic experimental probe is diboson resonance search in VBF.

Theoretical origin of common feature:

Unitarization of $WW \rightarrow WW$, $WW \rightarrow ZZ$ scattering amplitudes



Graphic: S. Chivukula

- SM: Higgs exchange cancels E^2/v^2 term in amplitude.
- 2HDM/SM+singlet: cancellation \rightarrow sum rule $(\kappa_V^h)^2 + (\kappa_V^H)^2 = 1$
- Higher-isospin scalars: $(\kappa_V^h)^2 + (\kappa_V^H)^2 > 1$, need $H^{\pm\pm}$ and H^\pm in new u -channel diagrams: couplings inter-related

Falkowski, Rychkov & Urbano, 1202.1532 (see also Higgs Hunter's Guide)

Georgi-Machacek model Georgi & Machacek 1985; Chanowitz & Golden 1985

SM Higgs bidoublet + two isospin-triplets in a **bitriplet**:

$$\Phi = \begin{pmatrix} \phi^{0*} & \phi^+ \\ -\phi^{+*} & \phi^0 \end{pmatrix} \quad X = \begin{pmatrix} \chi^{0*} & \xi^+ & \chi^{++} \\ -\chi^{+*} & \xi^0 & \chi^+ \\ \chi^{++*} & -\xi^{+*} & \chi^0 \end{pmatrix}$$

Physical spectrum: Custodial symmetry fixes almost everything!

Bidoublet: $2 \times 2 \rightarrow 3 + 1$

Bitriplet: $3 \times 3 \rightarrow 5 + 3 + 1$

- Two custodial singlets mix $\rightarrow h^0, H^0$
- Two custodial triplets mix $\rightarrow (H_3^+, H_3^0, H_3^-) + \text{Goldstones}$
- Custodial fiveplet $(H_5^{++}, H_5^+, H_5^0, H_5^-, H_5^{--})$ unitarizes $VV \rightarrow VV$

Georgi-Machacek model Georgi & Machacek 1985; Chanowitz & Golden 1985

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$$\Phi = \begin{pmatrix} \phi^{0*} & \phi^+ \\ -\phi^{+*} & \phi^0 \end{pmatrix} \quad X = \begin{pmatrix} \chi^{0*} & \xi^+ & \chi^{++} \\ -\chi^{+*} & \xi^0 & \chi^+ \\ \chi^{++*} & -\xi^{+*} & \chi^0 \end{pmatrix}$$

Physical spectrum: Custodial symmetry fixes almost everything!

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Bitriplet: $3 \times 3 \rightarrow 5 + 3 + 1$

- Two custodial singlets mix $\rightarrow h^0, H^0$ m_h, m_H \leftarrow (very similar)
- Two custodial triplets mix $\rightarrow (H_3^+, H_3^0, H_3^-)$ m_3 \leftarrow to 2HDM)
- Custodial fiveplet $(H_5^{++}, H_5^+, H_5^0, H_5^-, H_5^{--})$ m_5 \leftarrow new!

Generalized Georgi-Machacek models

Galison 1984; Robinett 1985; HEL 1999; Chang et al 2012; HEL & Rentala 2015

Replace the bitriplet with a $bi-n$ -plet \implies “GGM $_n$ ”

Bidoublet: $2 \times 2 \rightarrow 3 + 1$

Bitriplet: $3 \times 3 \rightarrow 5 + 3 + 1$

Biquartet: $4 \times 4 \rightarrow 7 + 5 + 3 + 1$

Bipentet: $5 \times 5 \rightarrow 9 + 7 + 5 + 3 + 1$

Bisextet: $6 \times 6 \rightarrow 11 + 9 + 7 + 5 + 3 + 1$

Larger $bi-n$ -plets forbidden by perturbative unitarity of weak charges!

- Two custodial singlets mix $\rightarrow h^0, H^0$
- Two custodial triplets mix $\rightarrow (H_3^+, H_3^0, H_3^-) +$ Goldstones
- Custodial fiveplet $(H_5^{++}, H_5^+, H_5^0, H_5^-, H_5^{--})$ unitarizes $VV \rightarrow VV$
- Additional states

Phenomenology I: custodial singlets h^0, H^0

Vevs: $\langle \Phi \rangle = (v_\phi/\sqrt{2})I_{2 \times 2}$, $\langle X_n \rangle = v_n I_{n \times n} \implies$ define $c_H = v_\phi/v$

Recall $c_H^2 =$ fraction of $M_{W,Z}^2$ coming from doublet vev

Two custodial-singlet states are mixtures of $\phi^{0,r}$ and custodial singlet from higher-isospin scalars:

$$h^0 = c_\alpha \phi^{0,r} - s_\alpha H_1'^0, \quad H^0 = s_\alpha \phi^{0,r} + c_\alpha H_1'^0$$

Couplings to W^+W^-/ZZ and $\bar{f}f$:

$$\begin{aligned} \kappa_V^h &= c_\alpha c_H - \sqrt{A} s_\alpha s_H & \kappa_f^h &= c_\alpha / c_H \\ \kappa_V^H &= s_\alpha c_H + \sqrt{A} c_\alpha s_H & \kappa_f^H &= s_\alpha / c_H \end{aligned}$$

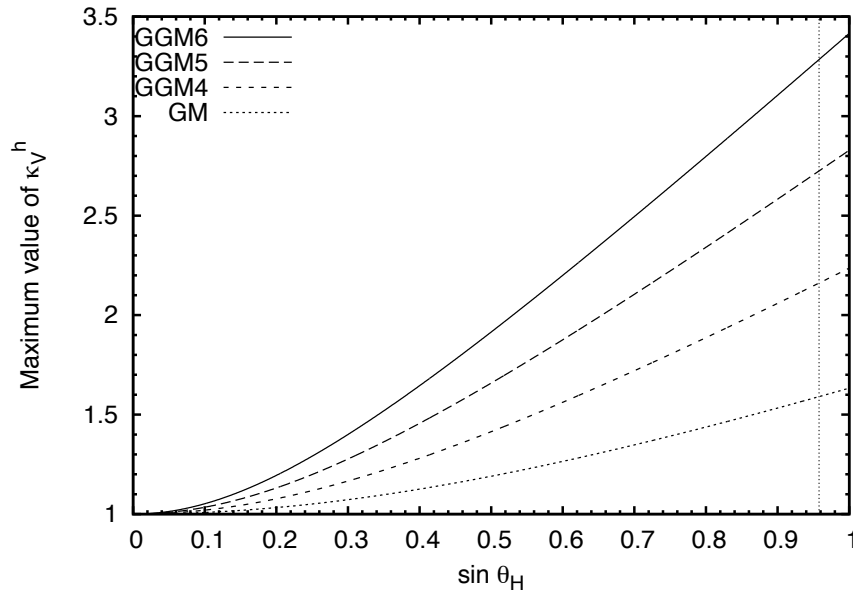
Note that $\kappa_V^h \leq [1 + (A-1)s_H^2]^{1/2}$, saturated when $\kappa_f^H = 0$.

\sqrt{A} factor comes from the generators: $A = 4T(T+1)/3$

$$A_{GM} = 8/3, \quad A_{GGM4} = 15/3, \quad A_{GGM5} = 24/3, \quad A_{GGM6} = 35/3$$

(Septet model: $A_7 = 16$)

Large enhancements of κ_V^h possible for large s_H (up to about 3.3):



Vertical line:

y_t perturbativity $\rightarrow \tan \theta_H < 10/3$

HEL & Rentala, 1502.01275

Impossible to have $\kappa_V^h, \kappa_f^h = 1$ without $s_H \rightarrow 0$:

High-precision measurements of Higgs couplings will constrain higher-isospin vacuum condensate.

$$\begin{aligned} \kappa_V^h &= c_\alpha c_H - \sqrt{A} s_\alpha s_H & \kappa_f^h &= c_\alpha / c_H \\ \kappa_V^H &= s_\alpha c_H + \sqrt{A} c_\alpha s_H & \kappa_f^H &= s_\alpha / c_H \end{aligned}$$

Phenomenology II: custodial triplet H_3^+, H_3^0, H_3^-

Couplings to fermions are the same as H^\pm, A^0 in Type-I 2HDM:

$$H_3^0 \bar{u}u : \quad \frac{m_u}{v} \tan \theta_H \gamma_5, \quad H_3^0 \bar{d}d : \quad -\frac{m_d}{v} \tan \theta_H \gamma_5,$$

$$H_3^+ \bar{u}d : \quad -i \frac{\sqrt{2}}{v} V_{ud} \tan \theta_H (m_u P_L - m_d P_R),$$

$$H_3^+ \bar{\nu} \ell : \quad i \frac{\sqrt{2}}{v} \tan \theta_H m_\ell P_R.$$

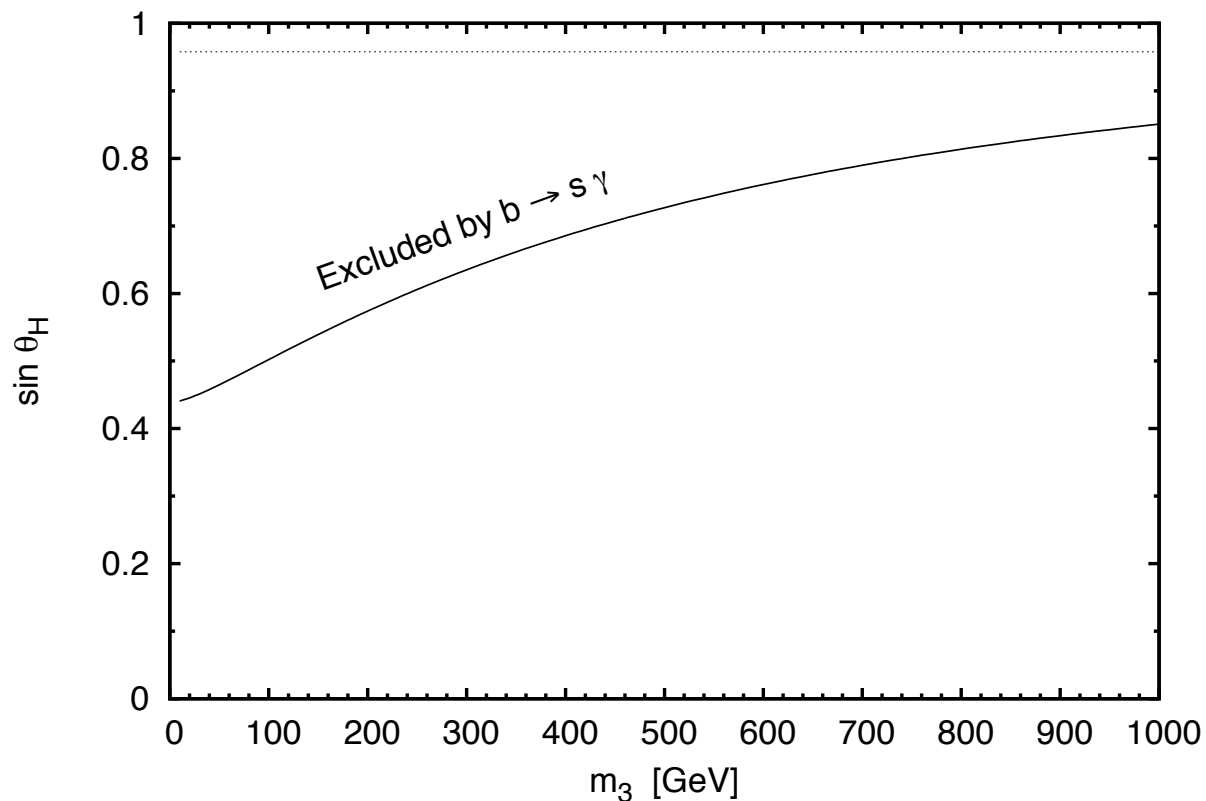
$Z H_3^+ H_3^-$ also the same as in 2HDM:

constraints from $b \rightarrow s\gamma$, $B_s \rightarrow \mu\mu$, R_b , etc translate directly.

Vector-phobic: no $H_3 VV$ couplings at tree level.

Constraint from $b \rightarrow s\gamma$

- H_3^+ in the loop: measurement constrains m_3 and $\sin\theta_H$
- Holds for all generalizations of Georgi-Machacek model
 - Also constrains septet model, but not identical



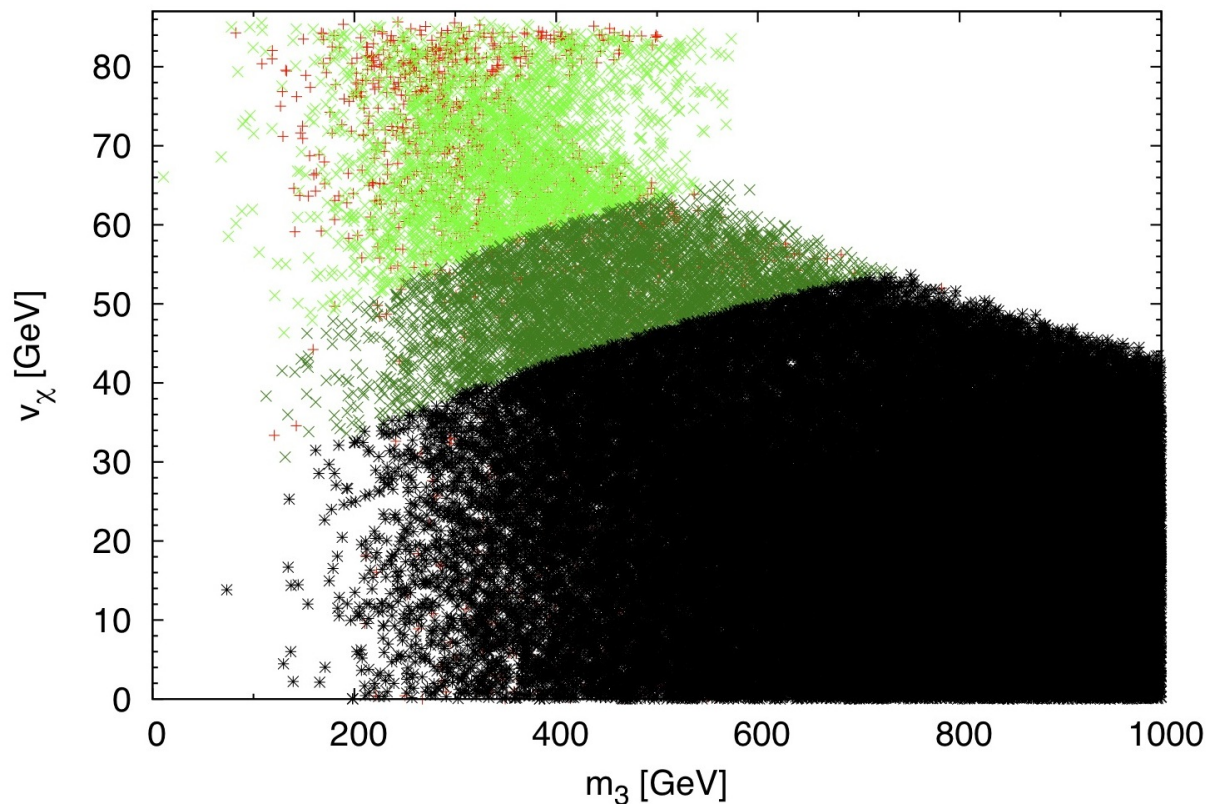
Hartling, Kumar & HEL, 1410.5538

Constraint from $b \rightarrow s\gamma$ in original Georgi-Machacek model:

Apply to original Georgi-Machacek model: $s_H^2 < 0.56$

Can constrain because high s_H at high m_3 is theoretically inaccessible.

\Rightarrow at least 44% of $M_{W,Z}^2$ is due to doublet vev (Model-dependent bound)



Hartling, Kumar & HEL, 1410.5538 (Light green points excluded by $b \rightarrow s\gamma$)

Phenomenology III: custodial fiveplet $H_5^{++}, H_5^+, H_5^0, H_5^-, H_5^{--}$

Custodial-fiveplet comes only from higher-isospin scalars:
no couplings to fermions!

$H_5 VV$ couplings are nonzero: very different from 2HDM!

$$\begin{aligned}
 H_5^0 W_\mu^+ W_\nu^- &: & -i \frac{2M_W^2}{v_{\text{SM}}} \frac{g_5}{\sqrt{6}} g_{\mu\nu}, \\
 H_5^0 Z_\mu Z_\nu &: & i \frac{2M_Z^2}{v_{\text{SM}}} \sqrt{\frac{2}{3}} g_5 g_{\mu\nu}, \\
 H_5^+ W_\mu^- Z_\nu &: & -i \frac{2M_W M_Z}{v_{\text{SM}}} \frac{g_5}{\sqrt{2}} g_{\mu\nu}, \\
 H_5^{++} W_\mu^- W_\nu^- &: & i \frac{2M_W^2}{v_{\text{SM}}} g_5 g_{\mu\nu},
 \end{aligned}$$

Coupling strength depends on the isospins of the scalars involved:

$$g_5^{\text{GM}} = \sqrt{2} s_H, \quad g_5^{\text{GGM4}} = \sqrt{\frac{24}{5}} s_H, \quad g_5^{\text{GGM5}} = \sqrt{\frac{42}{5}} s_H, \quad g_5^{\text{GGM6}} = \frac{8}{\sqrt{5}} s_H$$

Direct probe of higher-isospin vacuum condensate!

Phenomenology III: custodial fiveplet $H_5^{++}, H_5^+, H_5^0, H_5^-, H_5^{--}$

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 H_5^+ W_\mu^- Z_\nu &: & -i \frac{2M_W M_Z}{v_{\text{SM}}} \frac{g_5}{\sqrt{2}} g_{\mu\nu}, \\
 H_5^{++} W_\mu^- W_\nu^- &: & i \frac{2M_W^2}{v_{\text{SM}}} g_5 g_{\mu\nu},
 \end{aligned}$$

But g_5 is also fixed by $VV \rightarrow VV$ unitarization sum rule:

$$(\kappa_V^h)^2 + (\kappa_V^H)^2 - \frac{5}{6} g_5^2 = 1$$

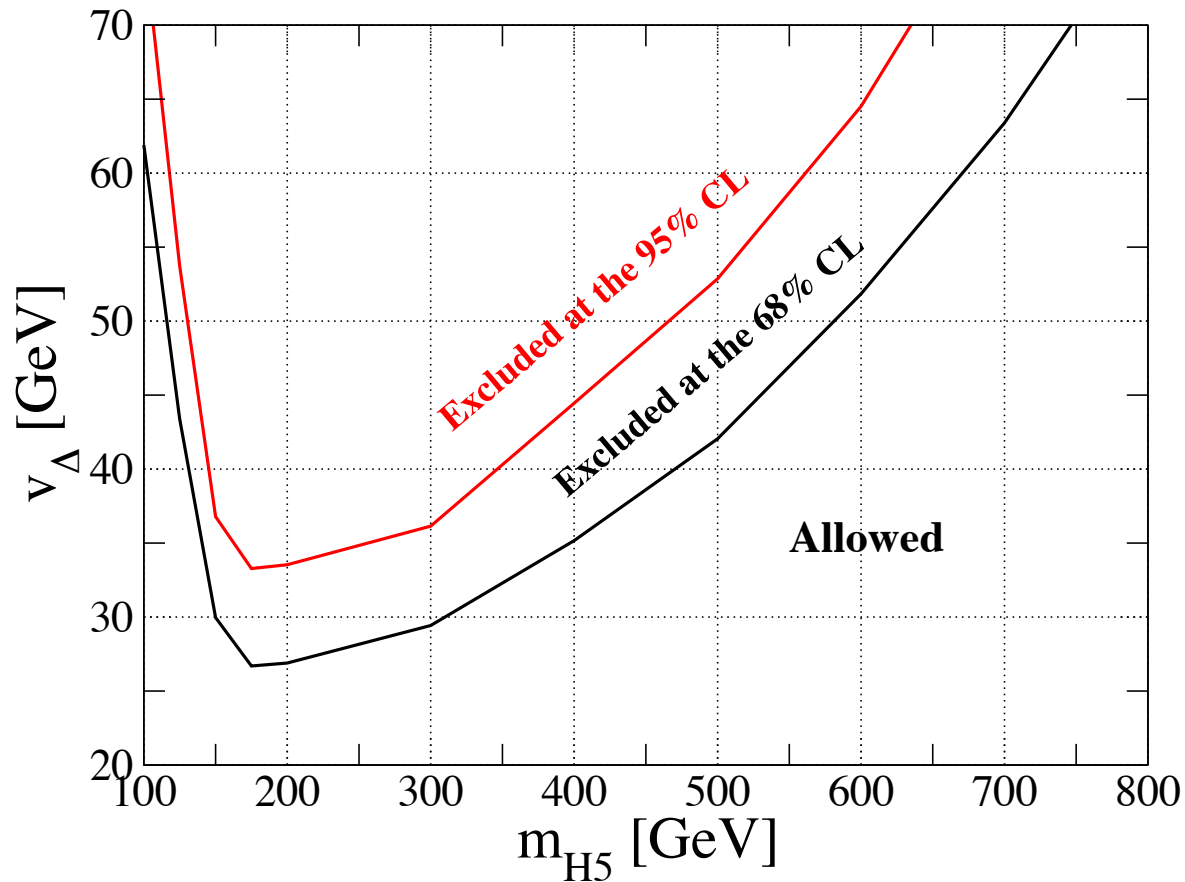
Falkowski, Rychkov & Urbano, 1202.1532 (see also Higgs Hunter's Guide)

(relies on custodial symmetry in scalar sector; same in *all* GGM models)

Constraint from VBF $H_5^{\pm\pm} \rightarrow W^\pm W^\pm \rightarrow$ same-sign dileptons

Theorist recasting of ATLAS $W^\pm W^\pm jj$ cross-section measurement [ATLAS, 1405.6241](#)

\Rightarrow put limit on VBF $\rightarrow H_5^{\pm\pm}$ cross section, directly constrain g_5



$$g_5 = \sqrt{2}s_H \text{ in GM model}$$

$$v_\Delta \equiv v_\chi = s_H v_{SM} / \sqrt{8}$$

[Chiang, Kanemura & Yagyu, 1407.5053](#)

What about higher H_5 masses?

Perturbative unitarity of finite part of $VV \rightarrow VV \Rightarrow$ upper bound on H_5 mass as function of s_H , just like SM Higgs mass bound!

- SM: $m_{h\text{SM}}^2 < 16\pi v_{\text{SM}}^2/5 \simeq (780 \text{ GeV})^2$ Lee, Quigg & Thacker 1977
- $SU(2)_L \times SU(2)_R$ -symmetric models:

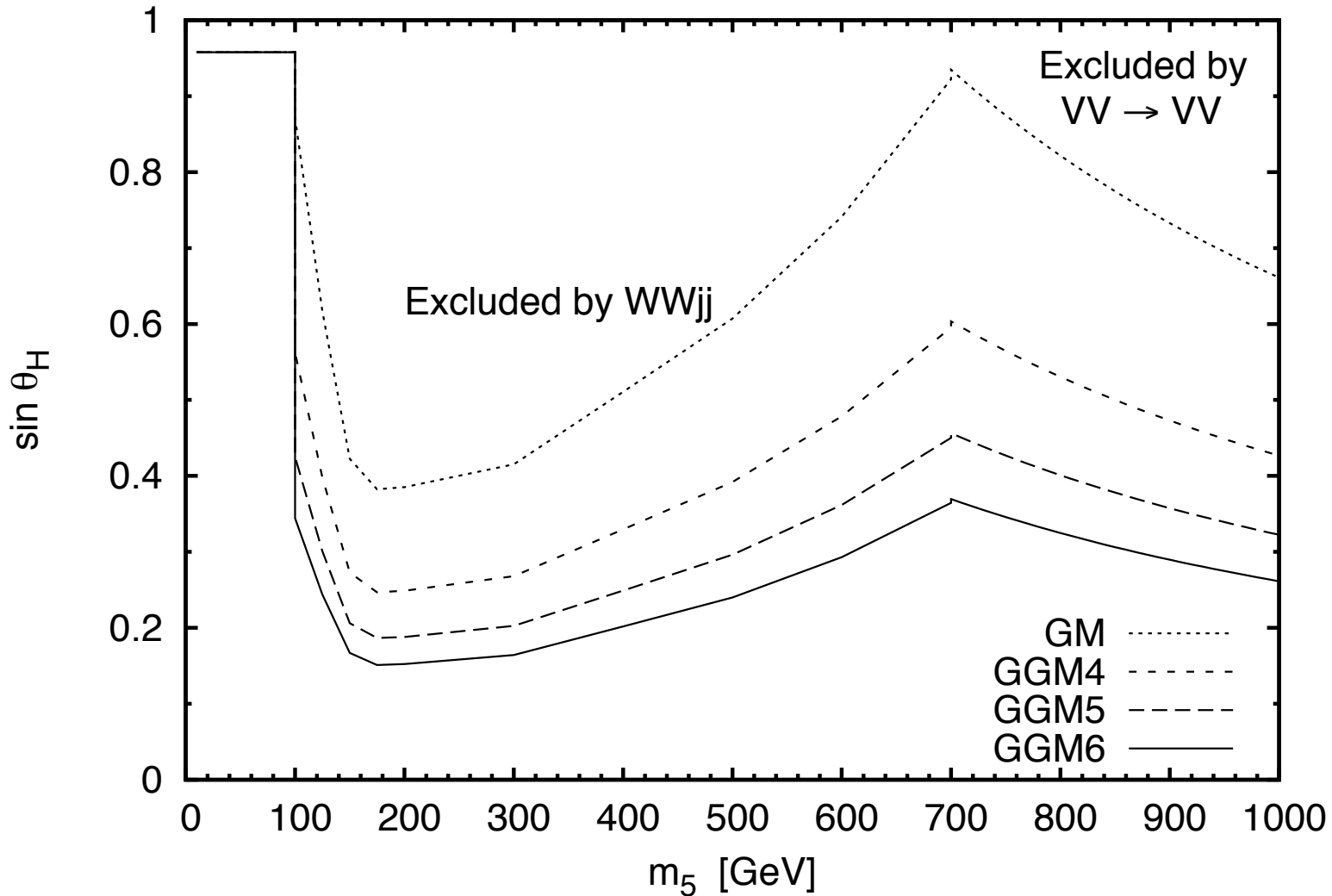
$$\left[(\kappa_V^h)^2 m_h^2 + (\kappa_V^H)^2 m_H^2 + \frac{2}{3} g_5^2 m_5^2 \right] < \frac{16\pi v_{\text{SM}}^2}{5}$$

Combine with $VV \rightarrow VV$ unitarization sum rule:

$$(\kappa_V^h)^2 + (\kappa_V^H)^2 - \frac{5}{6} g_5^2 = 1$$

Constraint is loosest (most conservative) when $\kappa_V^H \rightarrow 0$:

$$g_5^2 < \frac{6(16\pi v_{\text{SM}}^2 - 5m_h^2)}{5(4m_5^2 + 5m_h^2)} \simeq \frac{24\pi v_{\text{SM}}^2}{5m_5^2}$$



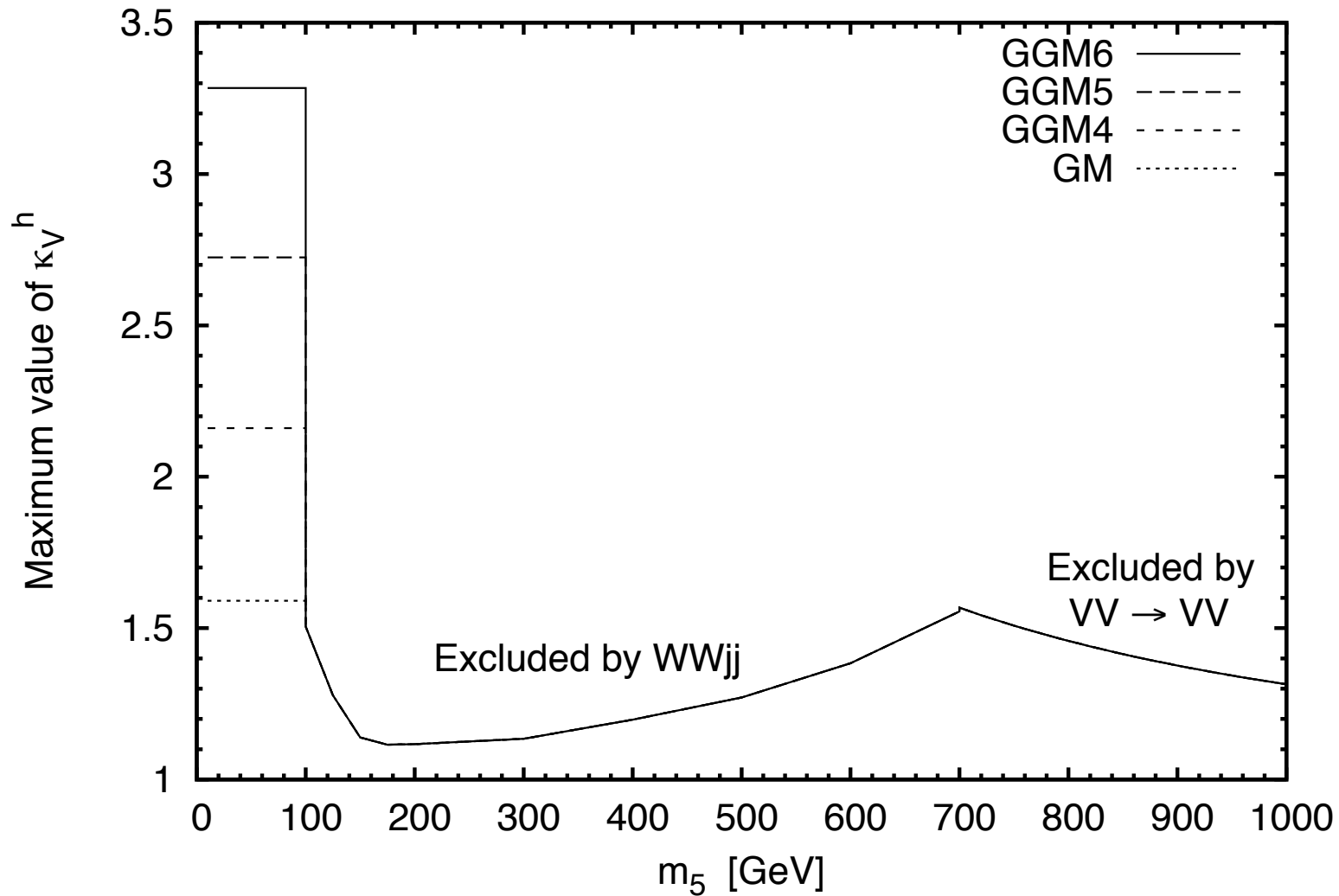
Complementary ranges of m_5 !

HEL & Rentala, 1502.01275

$$g_5^{\text{GM}} = \sqrt{2}s_H, \quad g_5^{\text{GGM4}} = \sqrt{\frac{24}{5}}s_H, \quad g_5^{\text{GGM5}} = \sqrt{\frac{42}{5}}s_H, \quad g_5^{\text{GGM6}} = \frac{8}{\sqrt{5}}s_H$$

Note: $s_H^2 \equiv$ exotic fraction of $M_{W,Z}^2$ is *least* constrained in original Georgi-Machacek model!

All the $SU(2)_L \times SU(2)_R$ models are the same when expressed in terms of g_5 : use sum rule, $(\kappa_V^h)^2 \leq 1 + 5g_5^2/6$

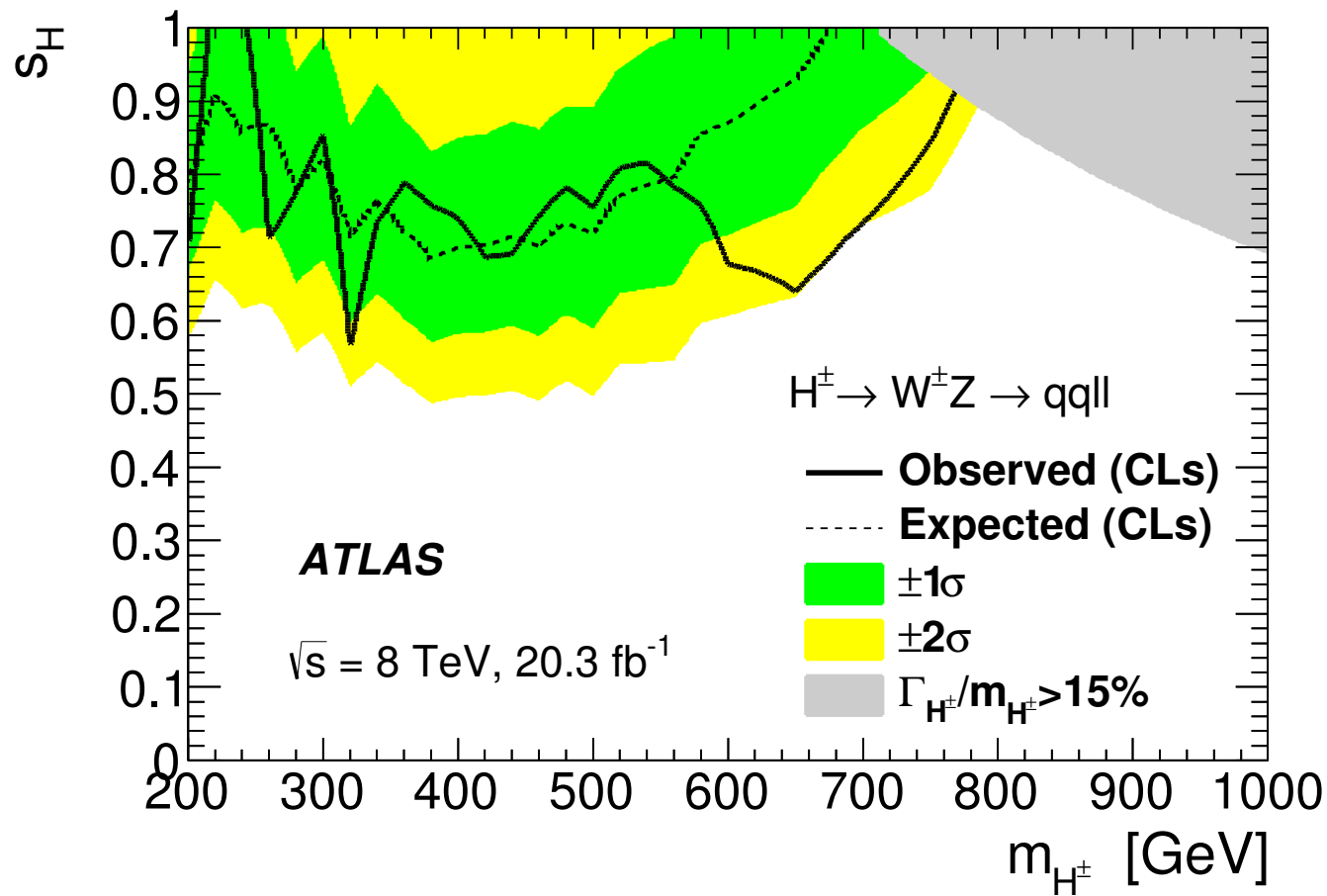


$\Rightarrow \kappa_V^h \lesssim 1.57$ for $m_5 > 100$ GeV

HEL & Rentala, 1502.01275

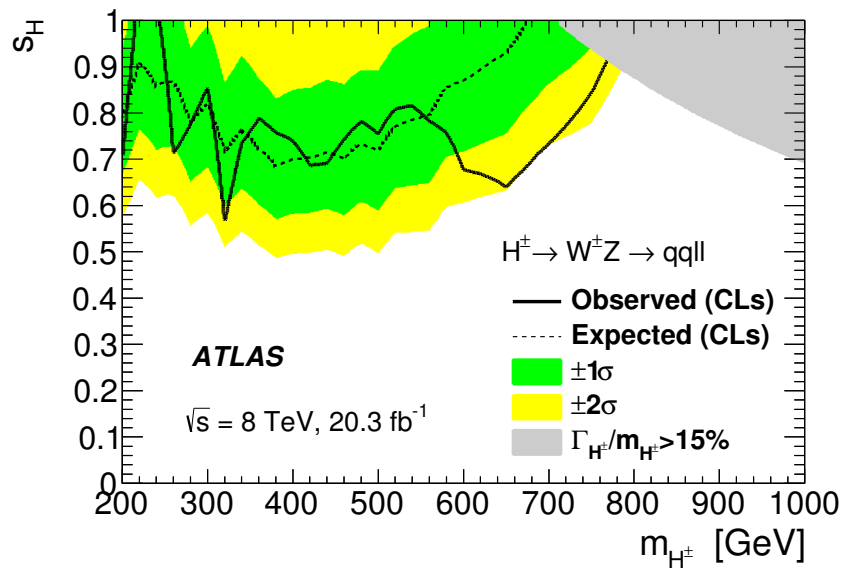
Constraint from VBF $H_5^\pm \rightarrow W^\pm Z \rightarrow qq\ell^+\ell^-$

Dedicated ATLAS search for singly-charged resonance in VBF, using Georgi-Machacek model as benchmark

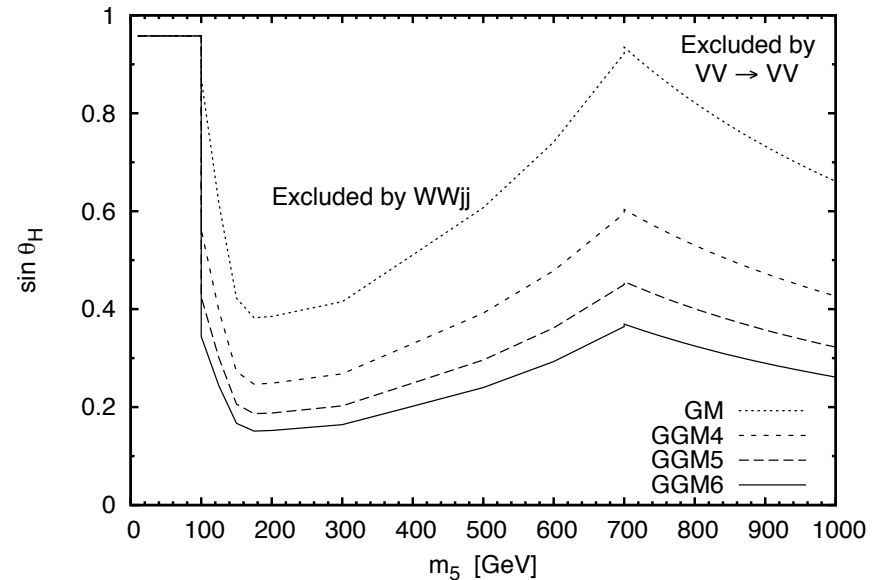


ATLAS 1503.04233

$H_5^\pm \rightarrow W^\pm Z$ exclusion not quite as strong as $H_5^{\pm\pm} \rightarrow W^\pm W^\pm$, but more data is coming.



ATLAS 1503.04233



HEL & Rentala, 1502.01275,

after Chiang, Kanemura & Yagyu, 1407.5053,

after ATLAS, 1405.6241

Straightforward to translate constraint from GM model to its higher-isospin generalizations.

What about lower H_5 masses?

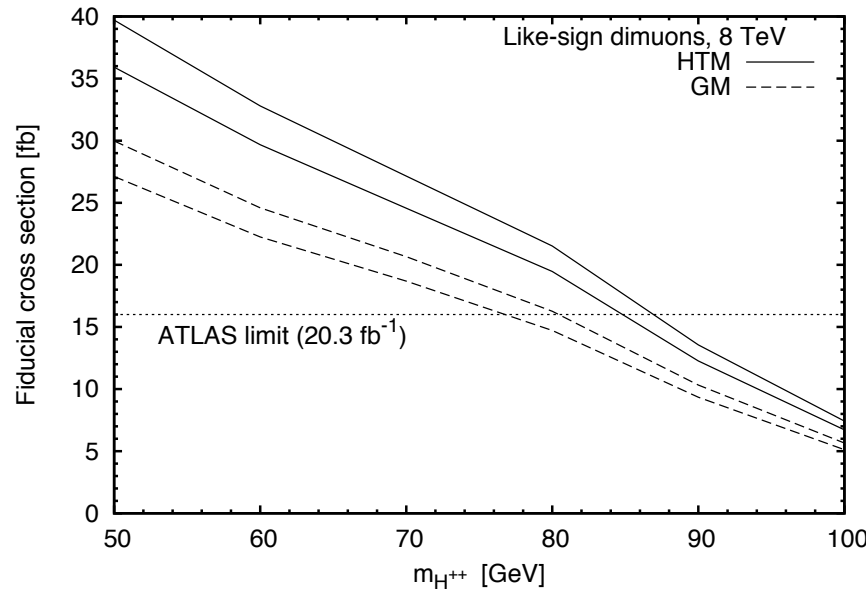
Constraint on $H^{\pm\pm}H^{\mp\mp} + H^{\pm\pm}H^{\mp}$ in Higgs Triplet Model from recasting ATLAS like-sign dimuons search [ATLAS, 1412.0237](#)

[Kanemura, Kikuchi, Yagyu & Yokoya, 1412.7603](#)

Adapt to generalized GM models using

$$\sigma_{\text{tot}}^{\text{NLO}}(pp \rightarrow H_5^{++}H_5^{--})_{\text{GM}} = \sigma_{\text{tot}}^{\text{NLO}}(pp \rightarrow H^{++}H^{--})_{\text{HTM}},$$

$$\sigma_{\text{tot}}^{\text{NLO}}(pp \rightarrow H_5^{\pm\pm}H_5^{\mp})_{\text{GM}} = \frac{1}{2}\sigma_{\text{tot}}^{\text{NLO}}(pp \rightarrow H^{\pm\pm}H^{\mp})_{\text{HTM}}.$$



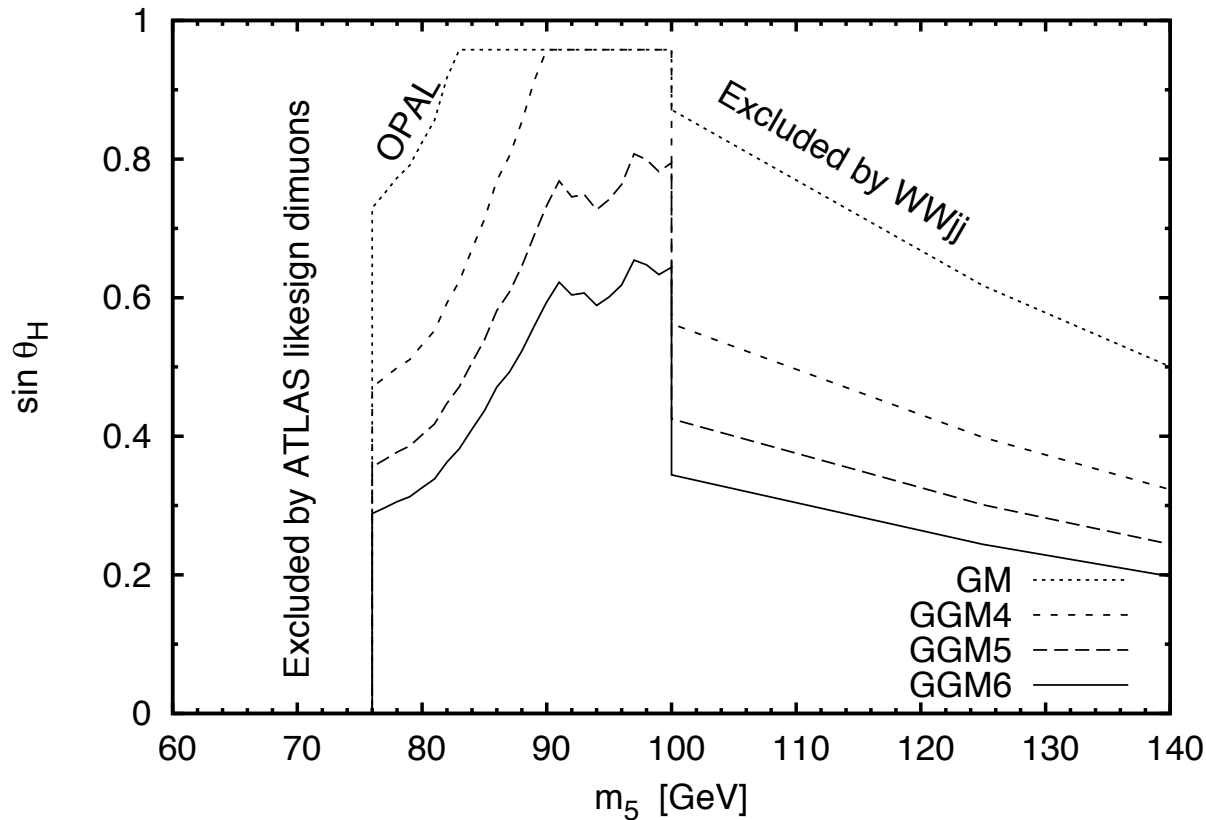
[HEL & Rentala, 1502.01275](#)

$\Rightarrow m_5 \gtrsim 76 \text{ GeV}$,
independent of g_5

Takes advantage of mass-degeneracy of H_5^{++} and H_5^+

What about lower H_5 masses?

Decay-mode-independent OPAL search for $Z + S^0$ production:
 constrain $H_5^0 ZZ$ coupling $\propto g_5$ OPAL, hep-ex/0206022



HEL & Rentala, 1502.01275; used HiggsBounds 4.2.0 for OPAL exclusion contour

Takes advantage of mass degeneracy H_5^0 and H_5^{++}

Septet model (work in progress)

Two CP-even neutral scalars:

$$h^0 = c_\alpha \phi^{0,r} - s_\alpha \chi^{0,r}, \quad H^0 = s_\alpha \phi^{0,r} + c_\alpha \chi^{0,r}$$

One CP-odd neutral scalar: ($c_H \equiv v_\phi/v_{\text{SM}}$ as usual)

$$A^0 = -s_H \phi^{0,i} + c_H \chi^{0,i}$$

Two charged scalars:

(one fermiophilic and one vectorphilic, but they mix in general)

$$H_f^+ = -s_H \phi^+ + c_H \left(\sqrt{\frac{5}{8}} \chi^{+1} - \sqrt{\frac{3}{3}} (\chi^{-1})^* \right),$$
$$H_V^+ = \sqrt{\frac{3}{8}} \chi^{+1} + \sqrt{\frac{5}{8}} (\chi^{-1})^*$$

A doubly-charged scalar, that couples to W^+W^+ :

$$H^{++} = \chi^{+2}$$

Some higher-charged states:

$$\chi^{+3}, \quad \chi^{+4}, \quad \chi^{+5}$$

- No H_5^0 ; would-be H_5^+ mixes with fermiophilic state
- Rely on H^{++} to constrain higher-isospin vacuum condensate

Septet model (work in progress)

$$H^{++}W_{\mu}^{-}W_{\nu}^{-} : i\frac{2M_W^2}{v_{\text{SM}}}(\sqrt{15}s_H)g_{\mu\nu}$$

VBF $H^{\pm\pm} \rightarrow W^{\pm}W^{\pm}$ is as good as ever!

VBF $H^{\pm} \rightarrow W^{\pm}Z$ loses its clean interpretation:

$H^+ \rightarrow \bar{f}f$ competes with W^+Z ; $m_{H^+} \neq m_{H^{++}}$ in general

No custodial symmetry:

- Unitarity bound on s_H at high $m_{H^{++}}$ is modified
- Sum-rule relationship between $H^{++}W^-W^-$ and hVV couplings is modified but these still remain useful.

Analysis of LHC constraints on septet-state pair production (trileptons; like-sign dileptons) excludes common masses $\lesssim 400$ GeV

Alvarado, Lehman & Ostdiek, 1404.3208

Summary & outlook

A higher-isospin component of the vacuum condensate is possible, but it can be constrained experimentally!

Essential signature is $H^{\pm\pm}$, H^\pm (and sometimes H_5^0) coupled to VV : searches in $VBF \rightarrow VV$ directly constrain the exotic vev.

Georgi-Machacek model makes a good benchmark: easy to reinterpret searches in higher-isospin generalizations.

Septet model is best constrained by using $H^{\pm\pm}$, since H^\pm can mix with fermiophilic state.

$VV \rightarrow VV$ unitarity constraint means that pushing $H^{\pm\pm}$ heavier forces exotic vev to be smaller.

The least constrained model at high $m_{H^{++}}$ is the original GM model: exotic fraction of $M_{W,Z}^2 \equiv s_H^2 \lesssim (675 \text{ GeV}/m_5)^2$.

BACKUP

Detail:

SM + real triplet ξ : $\rho > 1$

SM + complex triplet χ ($Y = 2$): $\rho < 1$

Combine them both: $\langle \chi^0 \rangle = v_\chi$, $\langle \xi^0 \rangle = v_\xi$; doublet $\langle \phi^0 \rangle = v_\phi/\sqrt{2}$

$$\rho = \frac{v_\phi^2 + 4v_\xi^2 + 4v_\chi^2}{v_\phi^2 + 8v_\chi^2} = 1 \text{ when } v_\xi = v_\chi$$

To avoid this being fine-tuned, enforce $v_\xi = v_\chi$ using a symmetry.

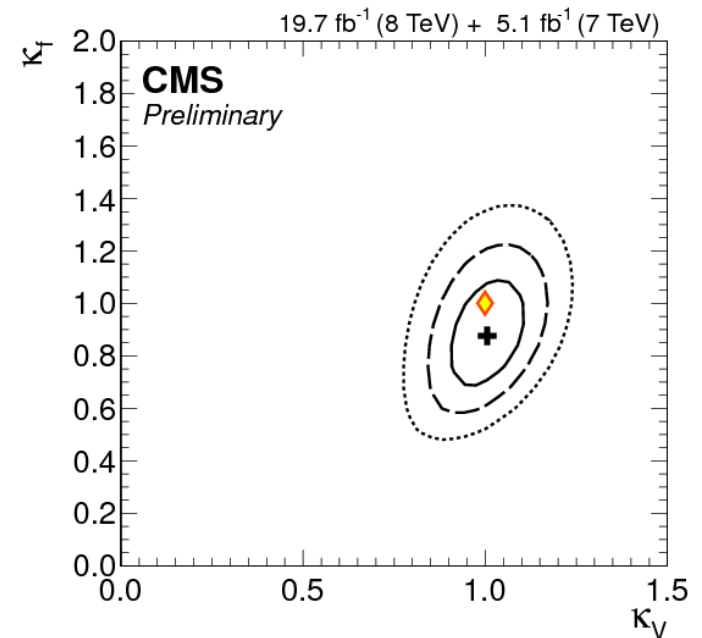
$SU(2)_L \times SU(2)_R$ global symmetry on scalar potential:

- present by accident in SM Higgs sector
- breaks to diagonal subgroup $SU(2)_{\text{custodial}}$ upon EWSB

Implementation of $\kappa_V^h > 1$

hVV coupling always **suppressed** in models with doublets/singlets:

- SM: $2i\frac{M_W^2}{v}g_{\mu\nu}$ ($v \simeq 246$ GeV)
- 2HDM: $2i\frac{M_W^2}{v}g_{\mu\nu} \sin(\beta - \alpha)$
- SM + singlet: $2i\frac{M_W^2}{v}g_{\mu\nu} \cos \alpha$ ($h = \phi \cos \alpha - s \sin \alpha$)



hWW coup can be **enhanced** in models with triplets (or larger):

- SM + **some multiplet X** : $2i\frac{M_W^2}{v}g_{\mu\nu} \cdot \frac{v_X}{v} 2 \left[T(T+1) - \frac{Y^2}{4} \right]$
($Q = T^3 + Y/2$)
- scalar with **isospin ≥ 1**
- must have a **non-negligible vev**
- must **mix into the observed Higgs h**

Motivation for enhanced hVV couplings

Simultaneous enhancement of all the h couplings can hide a non-SM contribution to the Higgs width.

LHC measures **rates** in particular final states:

$$\text{Rate}_{ij} = \frac{\sigma_i \Gamma_j}{\Gamma_{\text{tot}}} = \frac{\kappa_i^2 \sigma_i^{\text{SM}} \cdot \kappa_j^2 \Gamma_j^{\text{SM}}}{\sum_k \kappa_k^2 \Gamma_k^{\text{SM}} + \Gamma_{\text{new}}}$$

All rates will be identical to SM Higgs if all $\kappa_i \equiv \kappa \geq 1$ and

$$\kappa^2 = \frac{1}{1 - \text{BR}_{\text{new}}} \quad \text{BR}_{\text{new}} \equiv \frac{\Gamma_{\text{new}}}{\kappa^2 \Gamma_{\text{tot}}^{\text{SM}} + \Gamma_{\text{new}}}$$

Coupling enhancement hides presence of new decays!
New decays hide presence of coupling enhancement!

Constraint on Γ^{tot} (equivalently on κ) from off-shell $gg (\rightarrow h^*) \rightarrow ZZ$ assumes no new resonances in s -channel: a light H can cancel effect of modified h couplings. [1412.7577](#)

Study concrete models in which $\kappa > 1$ to gain insight.

Most general scalar potential:

Aoki & Kanemura, 0712.4053

Chiang & Yagyu, 1211.2658; Chiang, Kuo & Yagyu, 1307.7526

Hartling, Kumar & HEL, 1404.2640

$$\begin{aligned} V(\Phi, X) = & \frac{\mu_2^2}{2} \text{Tr}(\Phi^\dagger \Phi) + \frac{\mu_3^2}{2} \text{Tr}(X^\dagger X) + \lambda_1 [\text{Tr}(\Phi^\dagger \Phi)]^2 \\ & + \lambda_2 \text{Tr}(\Phi^\dagger \Phi) \text{Tr}(X^\dagger X) + \lambda_3 \text{Tr}(X^\dagger X X^\dagger X) \\ & + \lambda_4 [\text{Tr}(X^\dagger X)]^2 - \lambda_5 \text{Tr}(\Phi^\dagger \tau^a \Phi \tau^b) \text{Tr}(X^\dagger t^a X t^b) \\ & - M_1 \text{Tr}(\Phi^\dagger \tau^a \Phi \tau^b) (UXU^\dagger)_{ab} - M_2 \text{Tr}(X^\dagger t^a X t^b) (UXU^\dagger)_{ab} \end{aligned}$$

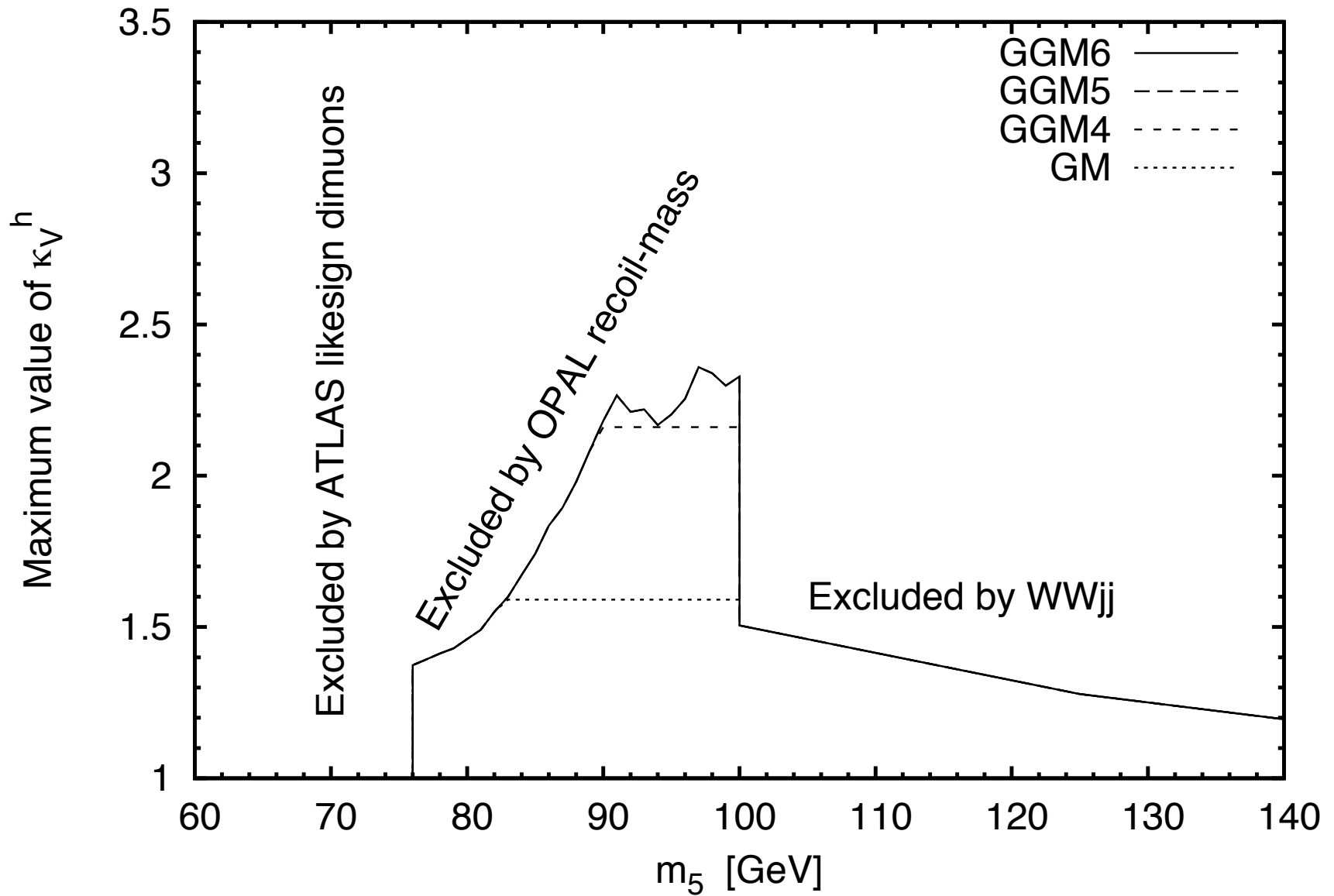
9 parameters, 2 fixed by M_W and $m_h \rightarrow$ free parameters are $m_H, m_3, m_5, v_\chi, \alpha$ plus two triple-scalar couplings.

Dimension-3 terms usually omitted by imposing Z_2 sym. on X .

These dim-3 terms are essential for the model to possess a decoupling limit!

$(UXU^\dagger)_{ab}$ is just the matrix X in the Cartesian basis of $SU(2)$, found using

$$U = \begin{pmatrix} -\frac{1}{\sqrt{2}} & 0 & \frac{1}{\sqrt{2}} \\ -\frac{i}{\sqrt{2}} & 0 & -\frac{i}{\sqrt{2}} \\ 0 & 1 & 0 \end{pmatrix}$$



$\Rightarrow \kappa_V^h \lesssim 2.36$ for all m_5 !

HEL & Rentala, 1502.01275

compare $\kappa_V^h \lesssim 3.3$ in unconstrained GGM6

2 deliverables in YR4 draft:

- A fully-specified benchmark scenario for direct H_5 searches
- Tables of VBF $\rightarrow H_5$ cross sections and decay widths

H5plane benchmark scenario:

- benchmark plane varying $m_5 \in [200, 3000]$ GeV and $s_H \in (0, 1)$

The 2 most relevant parameters for H_5 direct searches are input parameters.

All other input parameters are specified, including $m_h = 125$ GeV.

- compatible with spectrum calculator GMCALC [arXiv:1412.7387](https://arxiv.org/abs/1412.7387)

INPUTSET = 4: m_h, m_5, s_H, \dots are specified inputs

- satisfies theoretical constraints as much as possible

near-largest possible region of m_5 - s_H plane theoretically accessible (main challenge)

- Choose $m_3 > m_5$ so that $\text{BR}(H_5 \rightarrow VV) = 1$ at tree level

Higgs-to-Higgs $H_5 \rightarrow H_3V, H_3H_3$ decays are kinematically forbidden: avoid complications

Specification of H5plane benchmark scenario:

$$\begin{aligned}
 V(\Phi, X) = & \frac{\mu_2^2}{2} \text{Tr}(\Phi^\dagger \Phi) + \frac{\mu_3^2}{2} \text{Tr}(X^\dagger X) + \lambda_1 [\text{Tr}(\Phi^\dagger \Phi)]^2 + \lambda_2 \text{Tr}(\Phi^\dagger \Phi) \text{Tr}(X^\dagger X) \\
 & + \lambda_3 \text{Tr}(X^\dagger X X^\dagger X) + \lambda_4 [\text{Tr}(X^\dagger X)]^2 - \lambda_5 \text{Tr}(\Phi^\dagger \tau^a \Phi \tau^b) \text{Tr}(X^\dagger t^a X t^b) \\
 & - M_1 \text{Tr}(\Phi^\dagger \tau^a \Phi \tau^b) (U X U^\dagger)_{ab} - M_2 \text{Tr}(X^\dagger t^a X t^b) (U X U^\dagger)_{ab}.
 \end{aligned}$$

9 input parameters \Rightarrow trade $(\mu_2^2, \mu_3^2, \lambda_1, \lambda_5)$ for (G_F, m_5, m_h, s_H)

Fixed parameters	Variable parameters	Dependent parameters
$G_F = 1.1663787 \times 10^{-5} \text{ GeV}^{-2}$ $m_h = 125 \text{ GeV}$ $\lambda_3 = -0.1$ $\lambda_4 = 0.2$	$m_5 \in [200, 3000] \text{ GeV}$ $s_H \in (0, 1)$	$\lambda_2 = 0.4(m_5/1000 \text{ GeV})$ $M_1 = \sqrt{2} s_H (m_5^2 + v^2)/v$ $M_2 = M_1/6$

Table 6.1: Specification of the H5plane benchmark for the Georgi-Machacek model. These input parameters correspond to INPUTSET = 4 in GMCALC [252].

VBF $\rightarrow H_5$ cross sections (NNLO QCD, LO EW, onshell H_5)
and H_5 decay widths (LO) for $H_5^{++}, H_5^+, H_5^0, H_5^-, H_5^{--}$

Update of numbers in [LHCHSWG-2015-001](#) (H. Logan & M. Zaro),
already consistent with H5plane benchmark scenario

m_5 [GeV]	$\sigma_1^{\text{NNLO}}(H_5^0)$ [fb]	$\sigma_1^{\text{NNLO}}(H_5^+)$ [fb]	$\sigma_1^{\text{NNLO}}(H_5^-)$ [fb]	m_5 [GeV]	$\sigma_1^{\text{NNLO}}(H_5^{++})$ [fb]	$\sigma_1^{\text{NNLO}}(H_5^{--})$ [fb]
200.	1375. ^{+0.35%} _{-0.20%} $\pm 1.8\% \pm 0.51\%$	1770. ^{+0.30%} _{-0.18%} $\pm 1.6\% \pm 0.46\%$	1148. ^{+0.36%} _{-0.21%} $\pm 2.2\% \pm 0.54\%$	200.	2511. ^{+0.24%} _{-0.14%} $\pm 1.9\% \pm 0.40\%$	1070. ^{+0.33%} _{-0.21%} $\pm 2.9\% \pm 0.54\%$
210.	1288. ^{+0.33%} _{-0.19%} $\pm 1.8\% \pm 0.49\%$	1662. ^{+0.28%} _{-0.17%} $\pm 1.7\% \pm 0.45\%$	1073. ^{+0.34%} _{-0.21%} $\pm 2.2\% \pm 0.53\%$	210.	2364. ^{+0.24%} _{-0.14%} $\pm 1.9\% \pm 0.39\%$	997.0 ^{+0.31%} _{-0.20%} $\pm 2.9\% \pm 0.53\%$
220.	1209. ^{+0.30%} _{-0.18%} $\pm 1.8\% \pm 0.48\%$	1564. ^{+0.26%} _{-0.17%} $\pm 1.7\% \pm 0.44\%$	1004. ^{+0.32%} _{-0.20%} $\pm 2.2\% \pm 0.52\%$	220.	2229. ^{+0.23%} _{-0.13%} $\pm 1.9\% \pm 0.38\%$	930.3 ^{+0.29%} _{-0.19%} $\pm 3.0\% \pm 0.52\%$
230.	1136. ^{+0.28%} _{-0.17%} $\pm 1.8\% \pm 0.47\%$	1473. ^{+0.25%} _{-0.16%} $\pm 1.7\% \pm 0.43\%$	940.9 ^{+0.31%} _{-0.19%} $\pm 2.2\% \pm 0.51\%$	230.	2104. ^{+0.24%} _{-0.13%} $\pm 1.9\% \pm 0.37\%$	869.2 ^{+0.27%} _{-0.19%} $\pm 3.0\% \pm 0.51\%$
240.	1069. ^{+0.26%} _{-0.17%} $\pm 1.8\% \pm 0.46\%$	1388. ^{+0.25%} _{-0.15%} $\pm 1.7\% \pm 0.42\%$	883.0 ^{+0.29%} _{-0.18%} $\pm 2.3\% \pm 0.50\%$	240.	1988. ^{+0.24%} _{-0.12%} $\pm 1.9\% \pm 0.35\%$	813.3 ^{+0.25%} _{-0.18%} $\pm 3.0\% \pm 0.51\%$
250.	1006. ^{+0.27%} _{-0.16%} $\pm 1.8\% \pm 0.46\%$	1311. ^{+0.25%} _{-0.14%} $\pm 1.7\% \pm 0.41\%$	829.6 ^{+0.27%} _{-0.17%} $\pm 2.3\% \pm 0.49\%$	250.	1881. ^{+0.24%} _{-0.11%} $\pm 1.9\% \pm 0.34\%$	762.0 ^{+0.25%} _{-0.18%} $\pm 3.1\% \pm 0.50\%$
260.	948.9 ^{+0.27%} _{-0.15%} $\pm 1.8\% \pm 0.45\%$	1239. ^{+0.25%} _{-0.14%} $\pm 1.7\% \pm 0.40\%$	780.4 ^{+0.27%} _{-0.17%} $\pm 2.3\% \pm 0.48\%$	260.	1781. ^{+0.24%} _{-0.10%} $\pm 1.9\% \pm 0.33\%$	714.8 ^{+0.25%} _{-0.18%} $\pm 3.1\% \pm 0.49\%$

Uncert on σ from uncalculated NLO EW corrs $\simeq \pm 7\%$

m_5 [GeV]	$\Gamma_1^{\text{tot}}(H_5^{\pm\pm})$ [GeV]	$\Gamma_1^{\text{tot}}(H_5^\pm)$ [GeV]	$\Gamma_1^{\text{tot}}(H_5^0)$ [GeV]	BR($H_5^0 \rightarrow W^+W^-$)
200.	1.006	0.8608	0.8008	0.4187 ^{+14.4%} _{-14.4%}
210.	1.275	1.118	1.071	0.3969 ^{+15.4%} _{-14.4%}
220.	1.578	1.410	1.362	0.3863 ^{+15.4%} _{-14.4%}
230.	1.921	1.737	1.686	0.3799 ^{+15.4%} _{-14.4%}
240.	2.307	2.105	2.051	0.3749 ^{+15.4%} _{-15.4%}
250.	2.739	2.516	2.459	0.3714 ^{+16.4%} _{-15.4%}
260.	3.219	2.975	2.912	0.3685 ^{+16.4%} _{-15.4%}

Uncert on Γ from uncalculated NLO EW corrs $\simeq \pm 12\%$

s_H dependence incorporated via $\sigma \equiv s_H^2 \sigma_1$, $\Gamma \equiv s_H^2 \Gamma_1$

Update of numbers in [LHCHSWG-2015-001](#) (H. Logan & M. Zaro),
what's new:

- Used current YR4-recommended electroweak input parameters

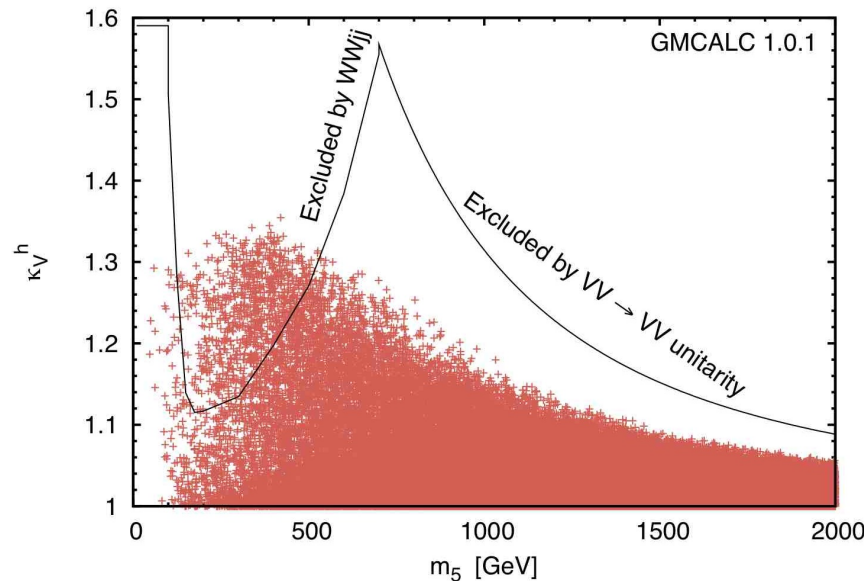
$$G_F = 1.1663787 \cdot 10^{-5} \text{ GeV}^{-2}, \quad M_W = 80.385 \text{ GeV}, \quad M_Z = 91.1876 \text{ GeV}, \\ \Gamma_W = 2.085 \text{ GeV}, \quad \Gamma_Z = 2.4952 \text{ GeV}.$$

- Used PDF4LHC NNLO parton dist'n fns with $\alpha_s(M_Z) = 0.118$, renorm & factorization scales set to M_W & varied by $[1/2, 2]$
- H_5 decay widths to VV (tree-level) now computed including doubly-offshell effects (GMCALC 1.2.0)
- Used YR4 recommended mass points for m_5 : 200–500 GeV in steps of 10 GeV, 500–3000 GeV in steps of 50 GeV

Summary & outlook

- ★ Custodial symmetry + unitarity sum rules extremely powerful!
 - VBF $H_5^\pm \rightarrow W^\pm Z$ search coming from ATLAS (Moriond?)
 - Weakest constraint: $m_5 \sim 76\text{--}100$ GeV. Offshell/loop decays?

★ High-mass $VV \rightarrow VV$ unitarity constraint is not saturated by full theory-constrained model: scan in GM model:



- perturb. unitarity of quartic couplings
- scalar potential bounded from below
- no deeper custodial-violating minima
- $b \rightarrow s\gamma$ constraint

Explicit scalar potentials for GGM models now available: full study feasible (but tedious)

★ Sum rules are different in septet model: no H_5^0 state, no custodial symmetry in scalar sector \implies under investigation